

## Exercises on code analysis techniques

### Abstract Interpretation (value set analysis)

In the following we consider abstract interpretation on programs using the interval abstract domain.

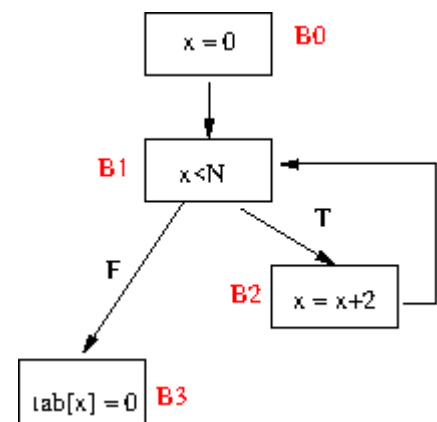
#### Exercise 1

We consider the following C code and its control-flow graph :

```
#define N 3
```

```
int x ;
int Tab[N] ;
```

```
x = 0 ;
while (x < N)
    x = x + 2 ;
    tab[x] = 0
```



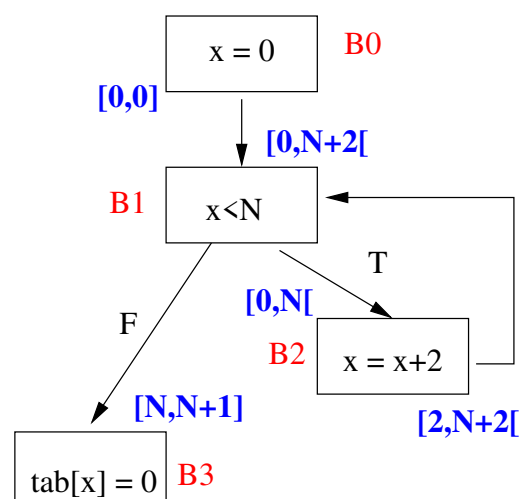
**Q1.** Compute the value sets at each entry/exit points of each basic blocks without using any acceleration technique (i.e., widening/narrowing).

**Q2.** Same as Q1, but using widening/narrowing operators.

**Q3.** Same as Q2 by replacing the constant 3 by the constants 1000 and 1001.

**Q4 .** What can we conclude about potential program vulnerabilities ?

**Solution:** the detail of the fix-point computations using intervals is available on Moodle, and the result is depicted on the Figure below. Hence, a buffer overflow will occur ...



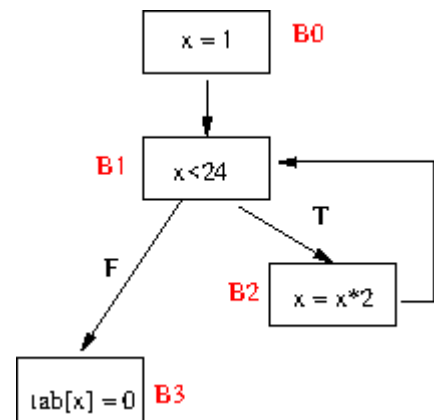
## Exercise 2

We consider the following C code and its control-flow graph :

```
#define N 33
```

```
int x ;  
int Tab[N] ;
```

```
x = 1;  
while (x<N)  
    x = x*2 ;  
tab[x] = 0
```



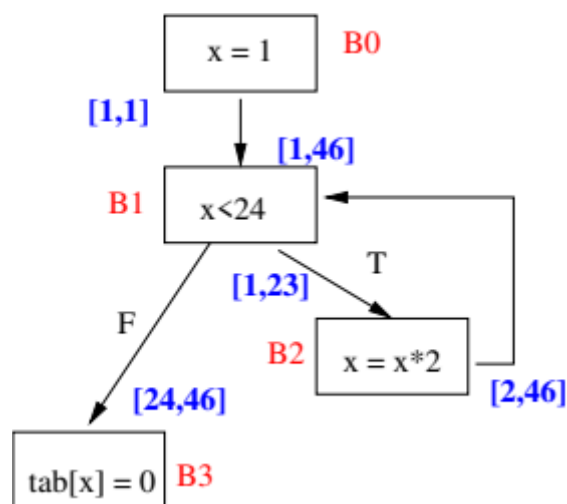
**Q1.** Compute the value sets at each entry/exit points of each basic blocks using acceleration techniques (i.e., widening/narrowing).

**Q2 .** What can we conclude about potential program vulnerabilities ?

**Q3.** How could we get more precise results with Frama-C ?

**Solution:**

Using fix-points computations with intervals (as in Exercise 1) we get the following result



The interval obtained when entering B3 is an over-approximation, the exact one would be [24,32].

Hence Frama-C would report a false positive for a potential buffer overflow in B3. A way to get more precise results is to use "slevel" or "loop-unrolling" options in order to unroll the loop 5 times before applying the widening operator ...

## Symbolic Execution

### Exercise 3

We consider the following code, where variable x is a user input :

```
#define N ...
unsigned x, y z ;
int T[N] ;

read(x) ;
z = 2*x ;
if (z<x+20) {
    y = z -10
    if (y > 12)
        T[y] = 0 ;
    else
        T[x] = 0 ;
} else {
    T[z+ 3] = 0 ;
}
```

**Q1.** Give its sets of execution paths and corresponding path predicates

PC1:  $z_0=2*x_0$  and  $z_0<x_0+20$  and  $y_0=z_0-10$  and  $y_0>12$   
PC2:  $z_0=2*x_0$  and  $z_0<x_0+20$  and  $y_0=z_0-10$  and  $y_0\leq 12$   
PC3:  $z_0=2*x_0$  and  $z_0\geq x_0+20$

**Q2.** Is there a valid input valuation for each of these path predicates ?

$x_0=30$  satisfies PC1  
 $x_0=10$  satisfies PC2  
 $x_0=21$  satisfies PC3

**Q3.** How to extend theses path predicates in order to detect potential buffer overflows ?

We have to add extra constraints on each PC, s.t. a BoF occurs if one of them is satisfiable:

PC1:  $z_0=2*x_0$  and  $z_0<x_0+20$  and  $y_0=z_0-10$  and  $y_0>12$  and  $(y<0$  or  $y\geq N)$   
PC2:  $z_0=2*x_0$  and  $z_0<x_0+20$  and  $y_0=z_0-10$  and  $y_0\leq 12$  and  $(x<0$  or  $x\geq N)$   
PC3:  $z_0=2*x_0$  and  $z_0\geq x_0+20$  and  $((z+3<0$  or  $(z+3)\geq N)$

## Exercise 4

We consider the following code example , where x is a **positive user input** :

```
#define N 3

int x ;
int Tab[N] ;

read (x) ;
while (x<N)
    x = x+2 ;
    tab[x] = 0
```

**Q1.** Is a symbolic tool like PathCrawler able to find **all** the execution paths triggering the vulnerability ? Explain your answer, giving the set of path predicates to consider and their corresponding solutions (assuming no arithmetic overflows)

There are 3 execution paths allowing to reach the potentially vulnerable statement `tab[x]=0`:

- entering an initial value for x larger than N

PC1 :  $x_0 \geq N$  and  $(x_0 < 0 \text{ or } x_0 \geq N)$ , satisfiable for any  $x_0 \geq N$

The buffer overflow is always triggered in this case (without arithmetic overflows).

Note that if we consider arithmetic overflows the BoF is not triggered for  $x_0$  in

$\{\text{UINT\_MAX}-1, \text{UINT\_MAX}, \text{UINT\_MAX}+1\}$

- unrolling the loop exactly once

PC2 :  $x_0 < N$  and  $x_1 = x_0 + 2$  and  $x_1 \geq N$ , satisfiable for  $x_0 = 1$  or  $x_0 = 2$ , hence triggering the BoF

- unrolling the loop twice

$x_0 < N$  and  $x_1 = x_0 + 2$  and  $x_1 < N$  and  $x_2 = x_1 + 2$  and  $(x_2 \geq N)$ , satisfiable for  $x_0 = 0$ , triggering the BoF

All of them could be found by a symbolic execution engine.

**Q2 .** Same question with  $N=1000$

For  $N=1000$ , the number of execution paths becomes quite large (about 1000 ... !).

It is still feasible to find all of them using a symbolic execution engine, but in practice it would depend on the exploration strategy ...