# Programming Language Semantics and Compiler Design

## Midterm Exam of Wednesday 27 October

- Duration: 1h20.
- 3 sheets of A4 paper are authorized.
- Any electronic device is forbidden.
- The grading scale is indicative.
- Exercises are independent.

- The care of your submission will be taken into account.
- It is recommended to read each exercise till the end before answering. Indicate your group number on your submission.
- If you don't know how to answer to some question, you may assume the result and proceed with the next question.
- The maximal grade is obtained with 20 points.

```
switch (a) {
begin
                                                                              case n1:
   var x := 42;
                                                                                 S1;
   var y := 21;
                                                                                 break;
                                     p := m ;
   proc p is x := x * 2
                                                                              case n2:
                                     acc := 1;
   proc q is y := y * 2;
                                                                                 S2;
                                     while acc <= n do
   call p;
                                        p := p + m ;
   begin
                                                                              case nk:
                                        acc := acc + 1
      proc q is x := x * 2;
                                                                                 Sk;
                                     od
      call q
                                                                                 break;
                                                                              default:
   end
                                          (b) Program for Exercise 2.
end
                                                                                 S
                                                                           }
    (a) Program for Exercise 1.
                                                                           (c) Example of program in Exercise 3.
```

Figure 1: Some code snippets.

#### Answer of exercise 1

- 1. It can be obtained following the same principle as in the course.
- 2. The semantics of the program does not change with static scope for variables and procedures. Statement call q calls the same procedure in both cases.

### Answer of exercise ??

1. Let us define  $S_0, S_1$  as the following sub-programs:

The invariant is:  $I \equiv p = acc \times m \land acc \leq n + 1$ .

```
• S_0: p := m; acc := 1, and
• S_1: p := p + m; acc := acc + 1, respectively.
```

We first show that the invariant propagates through the loop body and show that the condition obtained after the loop body implies the postcondition:

We consider the initialization and essentially show that before the loop, the initialization ensures the invariant.

$$\frac{\{m=m\}\;p:=m\;\{p=m\}\quad\{p=m\}\;acc:=1\;\{I\}}{\frac{\{m=m\}\;S_0\;\{I\}}{\{n\geq 1\}\;S_0\;\{I\}}}$$

Finally, using the rule for sequential composition, we obtain:

```
\frac{\{n\geq 1\}\;S_0\;\{I\}\quad\{I\}\;\;\text{while}\;acc\leq n\;\text{do}\;S_1\;\text{od}\;\{prod=m\times(n+1)\}}{\{n\geq 1\}\;S\;\{prod=m\times(n+1)\}}
```

#### Answer of exercise ??

1. An example of such program is given below:

```
switch (x + 2) {
   case 3:
      skip;
      break;
   case 2:
      x := x * y;
   default:
      x := 0
}
```

2. The grammar for case\_list is given below:

```
case_list ::= case n: S; break_option case_list | case n: S
where n is a denotation of a natural number and S is a statement.
```

3. The grammar for break\_option is given below:

o. The grammar for broam\_operion is given b

- 4. Non-terminal configurations are extended with a an integer that is the semantics of the arithmetic expression present in the swtich part. That is, the set of non-terminal configurations is a subset of  $\mathbf{Stm} \times \mathbf{State} \times \mathbb{Z}$ . In terminal configurations, one can find the state as well as a Boolean for recording whether a break statement has been encountered. That is, the set of terminal configurations is a subset of  $\mathbf{State} \times \mathbb{B}$ .
- 5. The rules are given below:

$$\begin{split} & (\mathtt{case\_list}, \sigma, v) \to (\sigma', b) \\ \hline & (\mathtt{case} \ \mathtt{n} : \mathtt{S}; \mathtt{break\_option} \ \mathtt{case\_list}, \sigma, v) \to (\sigma', b) \end{split} \ \mathcal{N}(n) \neq v \\ & \frac{(S, \sigma) \to \sigma'}{(\mathtt{case} \ \mathtt{n} : \mathtt{S}; \mathtt{break}; \ \mathtt{case\_list}, \sigma, v) \to (\sigma', \mathtt{tt})} \ \mathcal{N}(n) = v \\ & \frac{(S, \sigma) \to \sigma'}{(\mathtt{case\_list}, \sigma', v) \to (\sigma'', b)} \ \mathcal{N}(n) = v \end{split}$$

6. The semantic rules are given below:

$$\begin{split} & \qquad \qquad (\texttt{case\_list}, \sigma, \mathcal{A}[a]\sigma) \to (\sigma', \texttt{tt}) \\ \hline & (\texttt{switch}(a) \; \{\texttt{case\_list} \; \texttt{default\_option}\}, \sigma) \to \sigma' \\ & \qquad \qquad \qquad (\texttt{case\_list}, \sigma, \mathcal{A}[a]\sigma) \to (\sigma', \texttt{ff}) \\ & \qquad \qquad (\texttt{switch}(a) \; \{\texttt{case\_list} \; \}, \sigma) \to \sigma' \\ \hline & \qquad \qquad \qquad \underbrace{(\texttt{case\_list}, \sigma, \mathcal{A}[a]\sigma) \to (\sigma', \texttt{ff}) \quad (S, \sigma') \to \sigma''}_{\{\texttt{switch}(a) \; \{\texttt{case\_list} \; \texttt{default} : S\}, \sigma) \to \sigma''} \end{split}$$