B Method

We consider the B Abstract State Machine given below, which implements a system for processing administrative files. Each file is first received and can then either be validated or discarded.

```
MACHINE
                         File_Processing
SETS
                         FILES
VARIABLES
                         received, valid
INVARIANT
                         received \subseteq FILES \land valid \subseteq received
INITIALISATION
                         received := \emptyset; valid := \emptyset
OPERATIONS
                         receive (f) =
                            PRE f \in FILES
                            THEN received := received \cup \{f\}
                            END;
                          validate (f) =
                            PRE f \in \text{received}
                            THEN valid := valid \cup \{f\}
                            END;
                          \operatorname{discard}\left(f\right) =
                            PRE f \in \text{received}
                            THEN received := received \ \{f\}
                              END;
```

- 1. Write the proof obligation which should guarantee that the invariant is true after initialization. Is it correct? If not, how can the machine be corrected? Please justify your answer.
- 2. Write the proof obligation which should guarantee that the operation receive preserves the invariant. Is it correct? If not, how can the machine be corrected? Please justify your answer.
- 3. Write the proof obligation which should guarantee that the operation discard preserves the invariant. Is it correct? If not, how can the machine be corrected? Please justify your answer.