

Programming Language Semantics and Compiler Design
(Sémantique des Langages de Programmation et Compilation)
Generation of Assembly Code

Frédéric Lang & Laurent Mounier
`firstname.lastname@univ-grenoble-alpes.fr`
Univ. Grenoble Alpes, Inria,
Laboratoire d'Informatique de Grenoble & Verimag

Master of Sciences in Informatics at Grenoble (MoSIG)
Master 1 info

Univ. Grenoble Alpes - UFR IM²AG
`www.univ-grenoble-alpes.fr` — `im2ag.univ-grenoble-alpes.fr`

Outline - Generation of Assembly Code

Introduction

Machine “M”

Code Generation for Language **While**

Code Generation for Language **Proc**

Bonus: code Generation for Language **Block**

Summary

Outline - Generation of Assembly Code

Introduction

Machine “M”

Code Generation for Language **While**

Code Generation for Language **Proc**

Bonus: code Generation for Language **Block**

Summary

Main issues for code generation

- ▶ input: (well-typed) source pgm AST (or intermediate code)
- ▶ output: machine level code (assembly, relocatable, or absolute code)

Expected properties for the output

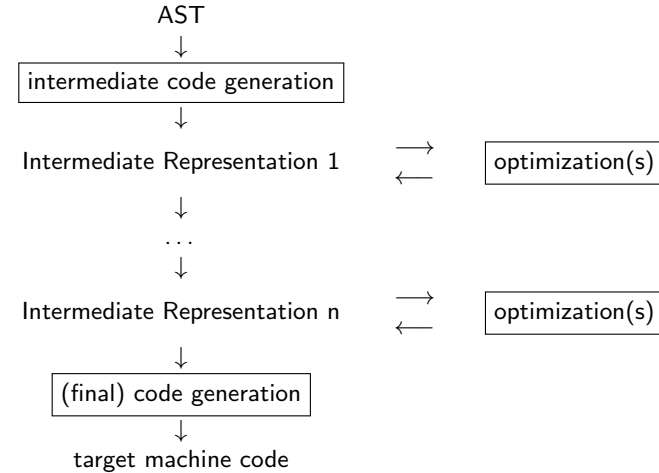
- ▶ **compliance** with the target machine instruction set, architecture, memory access, OS, ...
- ▶ **correctness** of the generated code semantically equivalent to the source pgm
- ▶ **optimality** w.r.t. non-functional criteria execution time, memory size, energy consumption, ...
- ▶ and **security** w.r.t. external (cyber-)attacks hardened code, no information leakage, checks for vulnerability detection, ...

Main issues for code generation (ctd)

Tasks of the Code Generator

- ▶ **Instruction selection:** choosing appropriate target-machine instructions to implement the (IR) statements.
Complexity depends on:
 - ▶ how abstract is the IR,
 - ▶ "expressiveness of instruction set" (e.g., support of some types),
 - ▶ expected quality of the output code according to some criteria (speed and size).
- ▶ **Registers allocation and assignment:** deciding what variables to keep in which registers at every location (when the target machine uses registers).
- ▶ **Instruction ordering:** deciding the scheduling order for the execution of instructions.
 - ▶ It affects the efficiency of the code and the required registers.
 - ▶ It is generally not possible to obtain an optimal (NP-complete) ⇒ heuristics

A pragmatic approach



Intermediate Representations

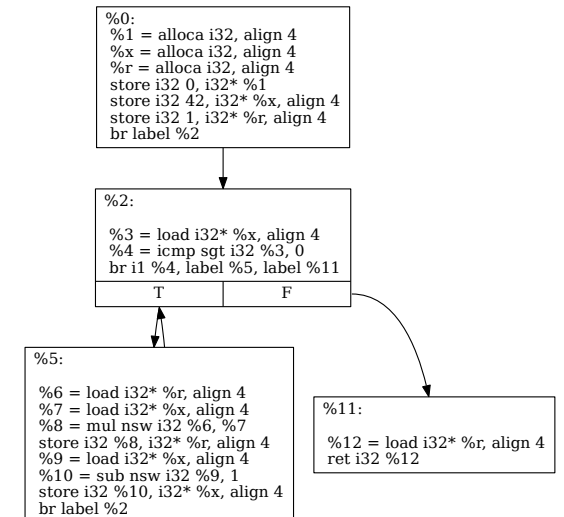
- ▶ Abstractions of a real target machine
 - ▶ generic code level instruction set
 - ▶ simple addressing modes
 - ▶ simple memory hierarchy
- ▶ Examples
 - ▶ a "stack machine"
 - ▶ a "register machine"
 - ▶ etc.

Remark Other intermediate representations are used in the optimization phases. □

Example 1: LLVM IR (register machine)

```

int main() {
  int x, r;
  x=42 ; r=1 ;
  while (x>0) {
    r = r*x;
    x = x-1;
  } ;
  return r ;
}
    
```



CFG for 'main' function

Example 2: Java ByteCode (stack machine)

```

public static int main(java.lang.String[]);
Code:
0: bipush      42
2: istore_1
3: iconst_1
4: istore_2
5: iload_1
6: ifle       20
9: iload_2
10: iload_1
11: imul
12: istore_2
13: iload_1
14: iconst_1
15: isub
16: istore_1
17: goto      5
20: iload_2
21: ireturn

public static int main() {
int x, r;
x=42 ; r=1 ;
while (x>0) {
    r = r*x;
    x = x-1;
} ;
return r ;
}

```

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language While

Code Generation for Language Proc

Bonus: code Generation for Language Block

Summary

Machine "M"

Machine with Registers

- ▶ Unlimited register set, $\{R_0, R_1, R_2, \dots\}$.
- ▶ Special registers:
 - ▶ program counter PC,
 - ▶ stack pointer SP,
 - ▶ frame pointer FP,
 - ▶ register R0 (contains always 0).
 (the exact purpose of these registers will become clear later)

Instructions, addresses, and integers take 4 bytes in memory.

Addressing

- ▶ Address of variable x is $E - \text{off}_x$ where:
 - ▶ E = address of the environment where x is defined
 - ▶ off_x = offset of x within this environment (statically computed, stored in the symbol table)
- ▶ Addressing modes:
 - R_i, val (immediate), $R_i +/- R_j$, $R_i +/- \text{offset}$

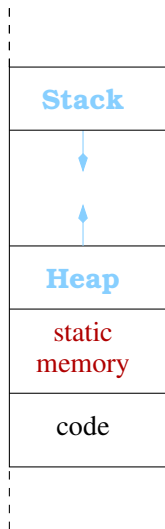
Instruction Set

- ▶ Usual arithmetic instructions OPER: ADD, SUB, AND, etc.
- ▶ Usual (conditional) branch instructions BRANCH: BA, BEQ (=), BGT (>), BLT (<), BGE (\geq), BLE (\leq), BNE (\neq).
- ▶ Usual calling instructions to labels or register: CALL.

instruction	informal semantics
OPER R_i, R_j, R_k	$R_i \leftarrow R_j \text{ oper } R_k$
OPER R_i, R_j, val	$R_i \leftarrow R_j \text{ oper val}$
CMP R_i, R_j	$R_i - R_j$ (set cond flags)
LD $R_i, [\text{adr}]$	$R_i \leftarrow \text{Mem}[\text{adr}]$
ST $R_i, [\text{adr}]$	$\text{Mem}[\text{adr}] \leftarrow R_i$
BRANCH label	if cond then $\text{PC} \leftarrow \text{label}$ else $\text{PC} \leftarrow \text{PC} + 4$

Run-Time Environment

Storage organization



- ▶ **Static data:**
 - ▶ computed at compile-time
 - ▶ allocated at load-time (once for all)
 - ▶ ex: global variables, constant strings, etc.
- ▶ **Dynamic data:**
 - ▶ in the stack
 - ▶ allocated with procedure activation
 - ▶ life-span: procedure execution
 - ▶ ex: local data of a proc. (parameters and local vars)
 - ▶ in the heap:
 - ▶ managed using malloc and free
 - ▶ life-span: from alloc to free (possibly after pgm termination)
 - ▶ ex: dynamic arrays

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language **While**

Code Generation for Language **Proc**

Bonus: code Generation for Language **Block**

Summary

Language **While**

Reminder

```

p ::= d ; s
d ::= var x | d ; d
s ::= x := a | s ; s | if b then s else s | while b do s od
a ::= n | x | a + a | a * a | ...
b ::= a = a | b and b | not b | ...

```

Remark Terms are well-typed.

→ distinction between boolean and arithmetic expr. □

Language **While**

Informal code generation

Informal code generation

Give the "Machine M" code for the following statements:

1. $y := x + 42 * (3+y)$
2. $\text{if (not } x=1) \text{ then } x := x+1$
 $\quad \text{else } x := x-1 ; y := x ; \text{fi}$

Functions for code generation

Notation

- ▶ $Code^*$: instruction sequences for machine “M”
- ▶ $\|$: concatenation operator for code and sequences of code

$GCStm : Stm \rightarrow Code^*$

$GCStm(s)$ computes the code C corresponding to statement s .

$GCAExp : Exp \rightarrow Code^* \times Reg$

$GCAExp(e)$ returns a pair (C, i) where C is the code allowing to

1. computes the value of e ,
2. stores it in R_i .

$GCBExp : BExp \times Label \times Label \rightarrow Code^*$

$GCBExp(b, ltrue, lfalse)$ produces the code C that computes the value of b and branches to label $ltrue$ when this value is “true” and to $lfalse$ otherwise.

Auxiliary functions

$AllocRegister : \rightarrow Reg$
allocates a new register R_i

$newLabel : \rightarrow Labels$
produces a new label

$GetOffset : Var \rightarrow \mathbb{Z}$
returns the offset corresponding to the specified name which depends on the position at which the variable is declared (shall be defined precisely for blocks and procedures)

Function $GCStm$

Assignments, sequential and iterative compositions

$GCStm(x := e)$	=	Let $(C, i) = GCAExp(e),$ $k = GetOffset(x)$ in $C \ ST\ R_i, [FP + k]$
$GCStm(s_1 ; s_2)$	=	Let $C_1 = GCStm(s_1),$ $C_2 = GCStm(s_2)$ in $C_1 \ C_2$
$GCStm(while\ e\ do\ s\ od)$	=	Let $lb = newLabel(),$ $ltrue = newLabel(),$ $lfalse = newLabel()$ in $lb : \ $ $GCBExp(e, ltrue, lfalse) \ $ $ltrue : \ $ $GCStm(s) \ $ $BA\ lb \ $ $lfalse :$

Function $GCStm$ (ctd)

Conditional statement

$GCStm(if\ e\ then\ s_1\ else\ s_2)$	=	Let $lnext = newLabel(),$ $ltrue = newLabel(),$ $lfalse = newLabel()$ in $GCBExp(e, ltrue, lfalse) \ $ $ltrue :$ $GCStm(s_1) \ $ $BA\ lnext \ $ $lfalse : \ $ $GCStm(s_2) \ $ $lnext :$
--------------------------------------	---	--

Function GCAexp

Arithmetic expressions

$GCAExp(x)$	=	Let	$i = \text{AllocRegister}()$ $k = \text{GetOffset}(x)$	
		in	$((LD\ R_i, [FP + k]), i)$	
$GCAExp(n)$	=	Let	$i = \text{AllocRegister}()$	
		in	$((ADD\ R_i, R_0, n), i)$	
$GCAExp(e_1 + e_2)$	=	Let	$(C_1, i_1) = GCAExp(e_1),$ $(C_2, i_2) = GCAExp(e_2),$ $k = \text{AllocRegister}()$	
		in	$((C_1 C_2 ADD\ R_k, R_{i_1}, R_{i_2}), k)$	

Function GCBexp

Boolean expressions

$GCBExp(e_1 = e_2, ltrue, lfalse)$	=	Let	$(C_1, i_1) = GCAExp(e_1),$ $(C_2, i_2) = GCAExp(e_2),$	
		in	$C_1 C_2 $ $CMP\ R_{i_1}, R_{i_2}$ $BEQ\ ltrue$ $BA\ lfalse$	
$GCBExp(e_1 \text{ and } e_2, ltrue, lfalse)$	=	Let	$l = \text{NewLabel}()$	
		in	$GCBExp(e_1, l, lfalse) $ $l: $ $GCBExp(e_2, ltrue, lfalse)$	
$GCBExp(\text{NOT } e, ltrue, lfalse)$	=		$GCBExp(e, lfalse, ltrue)$	

Similar principle for $e_1 > e_2$, $e_1 \geq e_2$, etc.

Exercises/Examples

Code generation

Assume that the offsets of variables x , y , and z are -4 , -8 , and -12 , respectively. Give the "Machine M" code for the following statements:

- if $x > 0$ then $z := x$ else $z := y$ fi
- $x := 10$; while $x > 10$ do $x := x - 1$ od

Adding new statements to **While**

Extend the code generation function

- ▶ to consider statements of the form repeat S until b ,
- ▶ to consider Boolean expressions of the form $b_1 \text{ xor } b_2$,
- ▶ to consider arithmetical expressions of the form $b ? e_1 : e_2$.

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language **While**Code Generation for Language **Proc**Syntax of **Proc**

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language **Block**

Summary

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language **While**

Code Generation for Language **Proc**

Syntax of **Proc**

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language **Block**

Summary

Syntax of Language **Proc**

Reminder

Procedure declarations:

$$Pgm ::= \dots \mid \mathbf{begin} D_V ; D_P ; S \mathbf{end}$$
$$D_P ::= \mathbf{proc} p (FP_L) \mathbf{is} D_V S \mathbf{end} D_P \mid \epsilon$$
$$FP_L ::= x, FP_L \mid \epsilon$$

Statements:

$$S ::= \dots \mid \mathbf{call} p(EP_L)$$
$$EP_L ::= AExp, EP_L \mid \epsilon$$

FP_L : list of formal parameters; EP_L : list of effective parameters

- ▶ only one single block, no nested procedures (\equiv C language)
- ▶ We assume (first) **value-passing** for **integer** parameters.

Example of program in **Proc**

```
begin
var z ; // global variable

proc p1 (x, y) is
  var t ; // local variable
  z := 42 ;
  t := x + y + z ;
end

proc p2 (x) is
  var z ; // local variable (hides the global one)
  call p1(x, 12) ; z := z+x ;
end

call p2(42) ; // main block body
end
```

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language **While**

Code Generation for Language **Proc**

Syntax of **Proc**

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language **Block**

Summary

Main issues for code generation with procedures

Procedure P is calling procedure Q . . .

Before the call:

- ▶ set up the memory environment of Q
- ▶ evaluate and “transmit” the effective parameters
- ▶ switch to the memory environment of Q
- ▶ branch to first instruction of Q

During the call:

- ▶ access to local/global variables
- ▶ access to parameter values

After the call:

- ▶ switch back to the memory environment of P
- ▶ resume execution to the instruction of P following the call

Outline - Generation of Assembly Code

Introduction

Machine “M”

Code Generation for Language **While**

Code Generation for Language **Proc**

Syntax of **Proc**

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language **Block**

Summary

Information exchanged between callers and callees?

- ▶ parameter values
- ▶ return address
- ▶ address of the caller memory environment (**dynamic link**)

This information should be stored in a memory zone:

- ▶ dynamically allocated
(exact number of procedure calls cannot be foreseen at compile time)
- ▶ accessible from both parties
(those addresses should be computable by the caller and the callee)

⇒

inside the **execution stack**, at **well-defined offsets** w.r.t FP

A possible “protocol” between the two parties

Before the call, the caller:

- ▶ evaluates the effective parameters
- ▶ pushes their values
- ▶ pushes the return address, and branch to the callee's 1st instruction

When it begins, the callee:

- ▶ pushes FP (**dynamic link**)
- ▶ assigns SP to FP (memory env. address)
- ▶ allocates its local variables on the stack

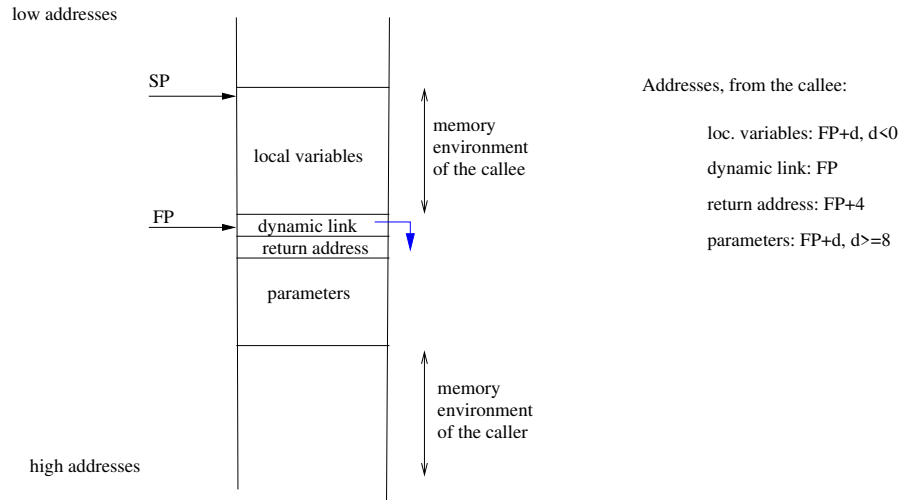
When it ends, the callee:

- ▶ de-allocates its local variables
- ▶ restores FP to caller's memory env. (**dynamic link**)
- ▶ branch to the return address, and pops it from the stack

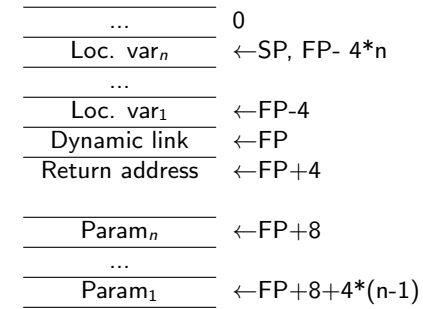
After the call, the caller

- ▶ de-allocates the parameters

Organization of the execution stack



Memory environment of the callee



Definition 1 (Offset of a variable or a parameter)

- ▶ For local variable var_i , as before, $GetOffset(var_i)$ is $-4 \times i$.
- ▶ For parameter $param_i$, $GetOffset(param_i)$ is $8 + 4 \times (n - i)$.

Instructions CALL and RET

- ▶ Assigning a code location (i.e., a label) to a register.
- ▶ Usual calling instructions to labels or register: CALL.
- ▶ Procedure return.

instruction	informal semantics
SET R label	$R \leftarrow @(label)$
CALL label	branch to the procedure labelled with label $PUSH(PC) \parallel PC \leftarrow label$
CALL R	branch to the address contained in register R $PUSH(PC) \parallel PC \leftarrow R$
RET	end of procedure: $PC \leftarrow MEM[SP] \parallel SP \leftarrow SP + 4$

Code generation for a procedure declaration

$GCProc : D_p \rightarrow Code^*$

$GCStm(dp)$ computes the code C corresponding to procedure declaration dp.

$$\overline{GCProc(\mathbf{proc} \ p \ (FP_L) \ \mathbf{is} \ s \ \mathbf{end})} = \text{Let} \quad \begin{array}{l} p = \text{newlabel}(), \\ C = GCStm(s) \end{array} \quad \text{in} \quad \begin{array}{l} p: \text{Prologue}(0) \parallel \\ C \parallel \\ \text{Epilogue} \end{array}$$

$$\overline{GCProc(\mathbf{proc} \ p \ (FP_L) \ \mathbf{is} \ dv ; s \ \mathbf{end})} =$$

$$\text{Let} \quad \begin{array}{l} p = \text{newlabel}(), \\ \text{size} = \text{SizeDecl}(dv), \\ C = GCStm(s) \end{array} \quad \text{in} \quad \begin{array}{l} p: \text{Prologue}(\text{size}) \parallel \\ C \parallel \\ \text{Epilogue} \end{array}$$

Remark $GCProc$ is applied to each procedure declaration. □

Code generation for a procedure declaration (ctd)

Prologue & Epilogue

Prologue (size):

```

push (FP)           ! dynamic link
ADD FP, SP, 0       ! FP := SP
ADD SP, SP, -size   ! loc. variables allocation

```

Epilogue:

```

ADD SP, FP, 0       ! SP := FP, loc. var. de-allocation
LD FP, [SP]         ! restore FP
ADD SP, SP, +4      ! erase previous backup of FP
RET                 ! return to caller

```

RET:

```
LD PC, [SP] // ADD SP, SP, +4
```

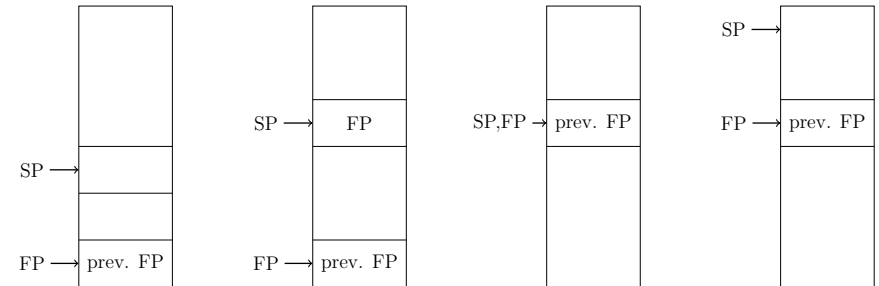
Illustration of the prologue

Prologue (size):

```

push (FP)           ! dynamic link
ADD FP, SP, 0       ! FP := SP
ADD SP, SP, -size   ! loc. variables allocation

```



Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language *While*Code Generation for Language *Proc*Syntax of *Proc*

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language *Block*

Summary

Code generation for a procedure call

Four steps:

1. evaluate and push each effective parameter
(with **passing-by-value mode** for now)
2. push the return address and branch to the callee
3. de-allocate the parameter zone

```

GCStm (call p (ep)) = Let (C, size) = GCParm(ep)
                      in
                        C ||
                        CALL p ||
                        ADD SP, SP, size

```

CALL p:

```
ADD R1, PC, +4 // Push (R1) // BA p
```

Code generation for the evaluation of parameters

$GCPParam : EP_L \rightarrow Code^* \times \mathbb{N}$

$GCStm(ep) = (c, n)$ where c is the code to evaluate and “push” each effective parameter of ep and n is the size of pushed data.

$GCPParam(\varepsilon)$	=	$(\varepsilon, 0)$
$GCPParam(a, ep)$	=	Let
		(Ca, i) = GCAexp(a),
		(C, size) = GCPParam(ep)
	in	(Ca Push(R_i) C, 4 + size)

Access to local/global variables?

```
begin
var z ; // global variable

proc p (x, y) is
    var t ; // local variable
    z := t+42 ;
end

z := 8 ;
call p(z, 12)
end
```

local variables

static offset w.r.t. the frame pointer FP
@t = FP-4 (within p environment)

global variables

- ▶ stored in a memory zone whose address @glob is fixed at load time
- ▶ static offset w.r.t @glob
@z = @glob - 4 (within the global variable memory area)

Outline - Generation of Assembly Code

Introduction

Machine “M”

Code Generation for Language While

Code Generation for Language Proc

Syntax of Proc

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language Block

Summary

Introducing parameters

Let f be a function whose effective parameter is at address FP-8.

Passing by value	Passing by address
LD R2, [FP-8]	ADD R2, FP, -8
push(R2)	push(R2)
CALL f	CALL f
ADD SP, SP, +4	ADD SP, SP, +4
Passing by result	Passing by value-result
ADD SP, SP, -4	LD R2, [FP-8]
CALL f	push(R2)
LD R2, [SP]	CALL f
ST R2, [FP-8]	LD R2, [SP]
ADD SP, SP, +4	ST R2, [FP-8]
	ADD SP, SP, +4

In practice: ABI (Application Binary Interface)

↔ to “standardize” how processor resources should be used
 ⇒ required to ensure compatibilities at binary level

- ▶ sizes, layouts, and alignments of basic data types
- ▶ **calling conventions**
argument & return value passing, saved registers, etc.
- ▶ system calls to the operating system
- ▶ the binary format of object files, program libraries, etc.

	Cleans Stack	Arguments	Arg Ordering
cdecl	Caller	On the Stack	Right-to-left
fastcall	Callee	ECX,EDX, then stack	Left-to-Right
stdcall	Callee	On the Stack	Left-to-Right
VC++ thiscall	Callee	EDX (this), then stack	Right-to-left
GCC thiscall	Caller	On the Stack (this pointer first)	Right-to-left

Figure: some calling conventions

Outline - Generation of Assembly Code

Introduction

Machine “M”

Code Generation for Language **While**

Code Generation for Language **Proc**

Syntax of **Proc**

Issues for Code Generation

A Protocol between the Caller and Callee

Code Generation

Other Modes for Passing Parameters

Example / Exercises

Bonus: code Generation for Language **Block**

Summary

Example

```
begin
var z ;

proc p1 () is
  z := 0 ;
  call p2(z+1, 3)
end ;

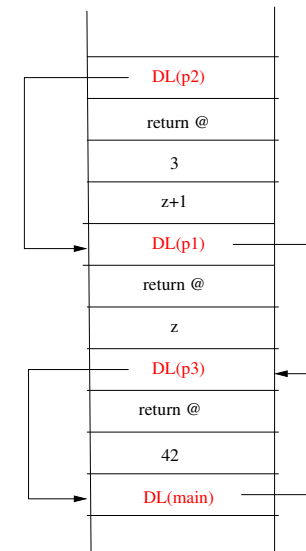
proc p2(x, y) is z := x + y end ;

proc p3 (x) is
  var z ;
  call p1() ; z := z+x
end

call p3(42)
end
```

- ▶ Give the execution stack when p2 is executed.
- ▶ Give the code for the block body and for procedures p1, p2 and p3.

Execution stack during the execution of p2



Global variable z is located on a dedicated memory area of base address @glob

The block body

Global variable z is at address @glob -4

```
var z ;
...
call p3(42) ;
```

Assembly code for the block body:

```
prologue(0) ! no local variables
! preparing the call p3(42)
! pushing 42
ADD R1, R0, #42 ! R1:=42
push (R1) ! push 1st parameter
CALL p3
ADD SP, SP, +4 ! clean the stack
epilogue()
```

Code for procedure p1

```
proc p1 () is
begin
z := 0 ;
call p2(z+1, 3) ;
end
```

Assembly code:

```
prologue(0) ! no local variables
! z := 0
ST R0, [@glob-4] ! z:=0
! call p2(z+1,3)
!compute and push z+1
LD R1, [@glob_4] ! R1:=z
ADD R2, R1, 1 ! R2:=z+1
push(R2) ! 1st param
! compute and push 3
ADD R3, R0, 3 ! R3:=3
push(R3) ! 2nd param
CALL p2
ADD SP, SP, 8 ! clean the stack
epilogue()
```

First example

Code for procedure p2

```
proc p2(x, y) is z := x + y ;
```

Assembly code:

```
prologue(0) ! no local variables
LD R1, [FP+12] ! R1:=x
LD R2, [FP+8] ! R2:=y
ADD R3, R1, R2 ! R3:=x+y
!assignment
ST R3, [@glob-4] ! z:=R3
epilogue()
```

First example

Code for procedure p3

```
proc p3 (x) is
begin
var z ;
call p1() ; z := z+x ;
end
```

Assembly code:

```
prologue(4) ! one local variable (z)
CALL p1
!compute z+x
LD R1, [FP-4] ! R1:=z
LD R2, [FP+8] ! R2:=x
ADD R2, R1, R2 ! R2:=z+x
ST R2, [FP-4] ! z:=R2
epilogue()
```

Procedures used as variables or parameters

```
var z1 ;
var p proc (int) ; /* p is a procedure variable */
proc p1 (x : int) is z1 := x ;
proc p2 (q : proc (int)) is call q(2) ;

p := p1 ;
call p ;
call p2 (p1) ;
```

Question: what code to produce

- ▶ for p := ... ?
- ▶ for call p ?
- ▶ for call p2(p1) ?

↔ we simply need the address of p1's 1st instruction

- ▶ variable p should store this information
- ▶ at code level, a **procedure type** is a **code address**

Exercise: code produced for the previous example ?

Vectors

↔ Adding 1-dimension integer arrays (= vectors):

```
p ::= d ; s
d ::= var x | var x[n] | d ; d
s ::= x := a | x[a] := a | s ; s | if b then s else s | while b do s od
a ::= n | x | x[a] | a + a | a * a | ...
b ::= a = a | b and b | not b | ...
```

- ▶ the size n of the array is a constant (**static arrays**, allocated in the stack)
- ▶ for array of size n , indices range from 0 to $n - 1$
- ▶ accessing an array outside its bound is incorrect (no semantics!)

Using arrays

```
var i ; var T[12] ;
i := 0 ;
while i < 12 do
  T[i] := i
od ;
i := T[i-5]
```

Array representation

$x[n]$ is a contiguous memory block of size $n \times 4$
 x denotes the address of first element $x[0]$
 address of i^{th} element of x is $x + 4 \times i$

↔ We extend function GCAExp to compute the **address** of $x[a]$:

```
GCAExp(x[a]) = Let i=AllocRegister()
                a=AllocRegister()
                b=AllocRegister()
                k=GetOffset(x)
                (C,j)=GCAExp(a)
            in   (C || computes a in Ri
                SUB Ra, FP, k || Ra := @x
                MUL Rb, Rj, 4 || Rb := a*4
                ADD Ri, Ra, Rb, i) Ri := @x + a*4
```

Exercise

```
begin
  var T[10] ;

  proc p (x[10], y) is
    var A[5] ;
    A[y-5] = x[y]
  end

  call p(T, 7) ;
end
```

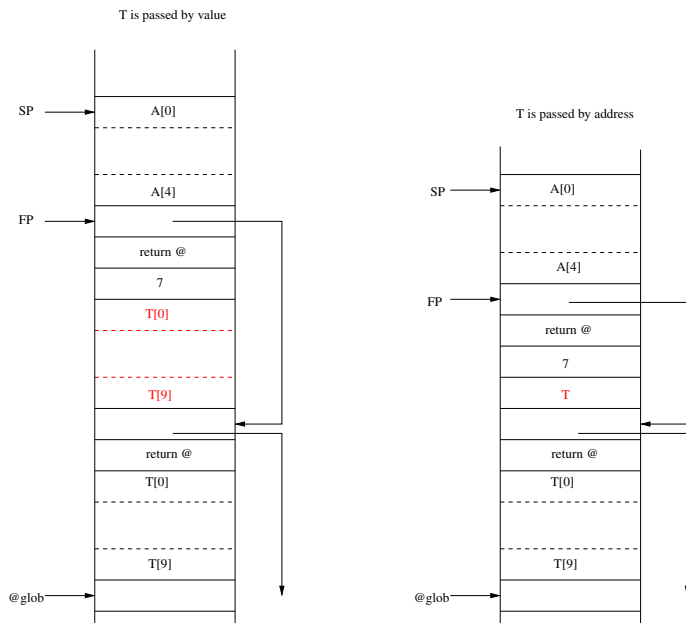
Questions

1. Draw the execution stack when procedure p is executed:
2. give the code produced when compiling this program

You should discuss these two situations:

- ▶ when parameter x is passed **by value**;
- ▶ when parameter x is passed **by address**.

Solution: Execution stack when p is executed



Solution: generated code

x passed by value

```

p:
Prologue(20)
LD R1, [FP+8] // R1:=y
SUB R2, R1, #5 // R2:=y-5
ADD R3, FP, 12 // R3:=@x
MUL R4, R1, 4 // R4:=y*4
ADD R5, R3, R4 // R5:=@(x[y])
SUB R6, FP, 20 // R6:=@A
MUL R7, R2, 4 // R6:=(y-5)*4
ADD R8, R6, R7 // R8:=@(A[y-5])
LD R9, [R5] // R9:=x[y]
ST R9, [R8] // A[y-5]:=x[y]
Epilogue
RET

```

```

// program body
... // push T[9], ... T[0]
ADD R1, R0, #7 // R1:=7
push(R1)
call p
ADD SP, SP, #44 // clean params

```

x passed by address

```

p:
Prologue(20)
LD R1, [FP+8] // R1:=y
SUB R2, R1, #5 // R2:=y-5
LD R3, [FP+12] // R3:=@T
MUL R4, R1, 4 // R4:=y*4
ADD R5, R3, R4 // R5:=@(T[y])
SUB R6, FP, 20 // R6:=@A
MUL R7, R2, 4 // R6:=(y-5)*4
ADD R8, R6, R7 // R8:=@(A[y-5])
LD R9, [R5] // R9:=T[y]
ST R9, [R8] // A[y-5]:=T[y]
Epilogue
RET

```

```

// program body
ADD R1, R0, #@glob // R1:=@glob
SUB R2, R1, #40 // R2:=@T
push(R2)
ADD R3, R0, #7 // R3:=7
push(R3)
call p
ADD SP, SP, #8 // clean params

```

Multi-dimensionnal arrays

↔ generalization to k dimension

```

d ::= var x | var x[n1][n2]...[nk] | d ; d
s ::= x := a | x[a1][a2]...[ak] := a | ...
a ::= n | x | x[a1][a2]...[ak] | ...

```

For var $x[n1][n2] \dots [nk]$:

- ▶ x denotes the address of a $n1 \times n2 \times \dots \times nk \times 4$ memory block
- ▶ $x[a1]$ is the addr. of the $(k-1)$ -dim. array $x[a1]([n2] \dots [nk])$
- ▶ $x[a1][a2]$ is the addr. of the $(k-2)$ -dim. array $x[a1][a2]([n3] \dots [nk])$
- ▶ etc.

Therefore:

$$\begin{aligned}
 @x[a1][a2] \dots [ak] &= @x \\
 &+ (a1 \times n2 \times n3 \times \dots \times nk \times 4) \\
 &+ (a2 \times n3 \times \dots \times nk \times 4) \\
 &+ \dots \\
 &+ (ak \times 4)
 \end{aligned}$$

Further extensions

Consider the following extensions to language **Proc**:

- ▶ functions ?
- ▶ pointers ?
- ▶ nested procedures ?
- ▶ objects ?
- ▶ etc.

↔ Have a look to code generated by **real compilers**
(<https://godbolt.org/>)

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language *While*

Code Generation for Language *Proc*

Bonus: code Generation for Language *Block*

Summary

Blocks

Syntax

$S ::= \dots \mid \mathbf{begin} D_V ; S \mathbf{end}$

$D_V ::= \mathbf{var} x \mid D_V ; D_V$

Remark Variables are not initialized and assumed to be of type **Int**. □

Problems raised for code generation

→ to preserve **scoping rules**:

- ▶ local variables should be visible inside the block,
- ▶ their lifetime should be limited to block execution.

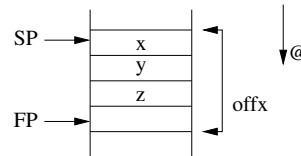
Possible locations to store local variables

→ registers vs **memory**

Storing local variables in memory - Example 1

Access to local variables within a block

```
begin
  var x ; var y ; var z ;
  ...
end
```



- ▶ A memory environment is associated to each declaration in D_V .
- ▶ Register FP contains the address of the current environment.
- ▶ (Static) offsets are associated to each local variables.

Definition 2 (Offset of a local variable)

The offset of a local variable is $-4 \times i$, where i is the position of the variable in the sequence of local declarations.

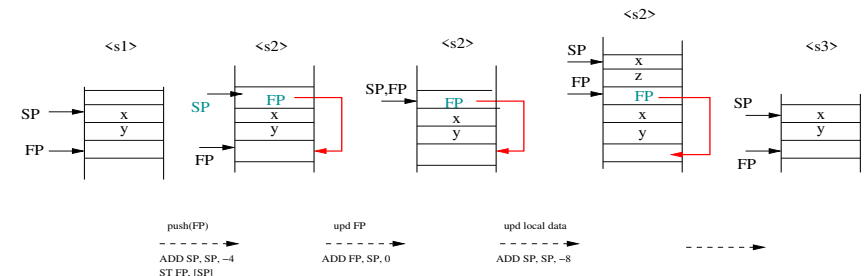
Example 1 (Offset of a local variable)

For var x ; var y ; var z ; : $\text{GetOffset}(z) = -4$, $\text{GetOffset}(y) = -8$, $\text{GetOffset}(x) = -12$.

Storing local variables in memory - Example 2

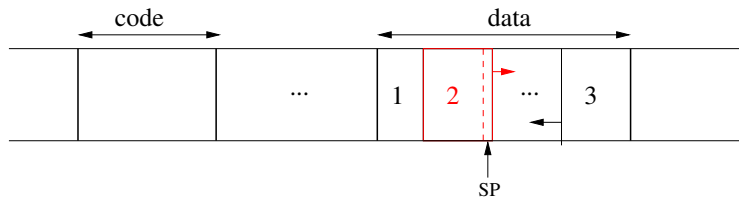
Access to local variables in case of nested blocks

```
begin
  var x ; var y ; <s1>
  begin
    var x ; var z ; <s2>
  end ;
  <s3>
end
```



- ▶ entering/leaving a block → allocate/de-allocate a mem. env.
 - ▶ nested block env. have to be linked together: **"Ariadne link"**
- ⇒ a **stack** of memory environments ... (~ **operational semantics**)

Structure of the memory



- 1: global variables
- 2: **execution stack**, SP = last occupied address
- 3: heap (for dynamic allocation)

Code generation for variable declarations

SizeDecl : $D_V \rightarrow \mathbb{N}$

SizeDecl(d) computes the size of declarations d

$\text{SizeDecl}(\text{var } x)$	$=$	4	(x of type Int)
$\text{SizeDecl}(d_1 ; d_2)$	$=$	Let	$v_1 = \text{SizeDecl}(d_1),$ $v_2 = \text{SizeDecl}(d_2)$
		in	$v_1 + v_2$

Code generation for blocks

$\text{GCStm}(\text{begin } d ; s ; \text{end})$	$=$	Let	$\text{size} = \text{SizeDecl}(d),$ $C = \text{GCStm}(s)$
		in	$\text{ADD SP, SP, -4} \parallel$ $\text{ST FP, [SP]} \parallel$ $\text{ADD FP, SP, 0} \parallel$ $\text{ADD SP, SP, -size} \parallel$ $C \parallel$ $\text{ADD SP, FP, 0} \parallel$ $\text{LD FP, [SP]} \parallel$ $\text{ADD SP, SP, 4} \parallel$

With the help of some auxiliary functions ...

prologue(size)	epilogue	push register (Ri)
ADD SP, SP, -4	ADD SP, FP, 0	ADD SP, SP, -4
ST FP, [SP]	LD FP, [SP]	ST Ri, [SP]
ADD FP, SP, 0	ADD SP, SP, +4	
ADD SP, SP, -size		

$\text{GCStm}(\text{begin } d ; s ; \text{end})$	$=$	Let	$\text{size} = \text{SizeDecl}(d),$ $C = \text{GCStm}(s)$
		in	$\text{Prologue}(\text{size}) \parallel$ $C \parallel$ Epilogue

Access to variables from a block?

```
...
begin
  var ...
  x := ...
end
```

What is the memory address of x ?

- ▶ if x is a **local** variable (w.r.t the current block)
 - ⇒ $\text{adr}(x) = \text{FP} + \text{GetOffset}(x)$
- ▶ if x is a **non local** variable
 - ⇒ it is defined in a “nesting” memory env. E
 - ⇒ $\text{adr}(x) = \text{adr}(E) + \text{GetOffset}(x)$
 - $\text{adr}(E)$ can be accessed through the “Ariadne link” ...

Access to non-local variables

The number n of indirections to perform on the “Ariadne link” depends on the “distance” between:

- ▶ the nesting level of the current block: p
- ▶ the nesting level of the target environment: r

More precisely:

- ▶ $r \leq p$
- ▶ $n = p - r$

⇒ n can be **statically** computed...

Remark The number of indirections can be statically computed because the programming language has a semantics with static bindings. □

Access to non-local variables: example

Example 2 (Access to non-local variables and number of indirections)

```
begin
  var x ; /* env. E1, nesting level = 1 */
  begin
    var y ; /* env. E2, nesting level = 2 */
    begin
      var z ; /* env. E3, nesting level = 3 */
      x := y + z /* s, nesting level = 3 */
    end
  end
end
```

From statement s :

- ▶ no indirection to access z
- ▶ 1 indirection to access y
- ▶ 2 indirections to access x

Code generation for variable access

1. the nesting level r of each identifier x is computed during type-checking;
2. it is associated to each occurrence of x in the AST (via the symbol table)
3. function GCStm keeps track of the current nesting level p (incremented/decremented at each block entry/exit)

$\text{adr}(x)$ is obtained by executing the following code:

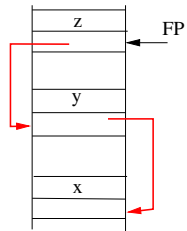
- ▶ if $r = p$:
 - $\text{FP} + \text{GetOffset}(x)$
- ▶ if $r < p$:
 - LD Ri, [FP
 - LD Ri, [Ri]} ($p - r - 1$) times
 - Ri + GetOffset(x)

Example (ctn'd)

```

begin
  var x ; /* env. E1, nesting level = 1 */
  begin
    var y ; /* env. E2, nesting level = 2 */
    begin
      var z ; /* env. E3, nesting level = 3 */
      x := y + z /* s, nesting level = 3 */
    end
  end
end
end

```



```

LD R1, [FP]    ! R1 = adr(E2)
LD R2, [R1 + offy] ! R2 = y
LD R3, [FP + offz] ! R3 = z
ADD R4, R2, R3  ! R4 = y+z
LD R5, [FP]
LD R5, [R5]    ! R5 = adr(E1)
ST R4, [R5 + offx] ! x = y + z

```

Code generated for statement s

An alternative for block variables

For code generation, all local variables of nested blocks can be **flattened**, i.e., shifted up to the **outermost block** environment

```

begin
  var x ; /* env. E1, nesting level = 1 */
  var y ; /* env. E2, nesting level = 2 */
  var z ; /* env. E3, nesting level = 3 */
  begin
    begin
      x := y + z /* s, nesting level = 3 */
    end
  end
end
end

```

⇒ all variable addresses are relative to env. E1:

- ▶ no need to push/pop FP at each block entry/exit (no prologue/epilogue)
- ▶ no need to generate code for computing variable addresses at runtime

Demo: code generation for nested blocks

Outline - Generation of Assembly Code

Introduction

Machine "M"

Code Generation for Language **While**Code Generation for Language **Proc**Bonus: code Generation for Language **Block**

Summary

Summary - Generation of Assembly Code

(Machine) Code generation from **While**, **Block**, and **Proc**

- ▶ Expected properties of the generated code: compliance, correctness, optimality.
- ▶ Machine M (with registers) and its instruction set.
- ▶ Formal code-generation functions.
- ▶ (non nested) Procedures.
- ▶ Calling conventions.
- ▶ (static) Arrays